

Solutions
Version 1

1. (3 Points) The keyword ____ is used in the class declaration of a subclass to indicate its superclass.
 - a. inherits
 - b. extends**
 - c. implements
 - d. super

2. (3 Points) Assuming a linked list of n nodes, the code fragment:

```
Node curr = head;
while (curr != null) {
    System.out.println(curr.getItem());
    curr.setNext(curr.getNext());
} // end while
```

requires _____ assignments.
 - a. n
 - b. $n - 1$
 - c. $n + 1$**
 - d. 1

3. (3 Points) If a problem of size n requires time that is directly proportional to n , the problem is _____.
 - a. $O(1)$
 - b. $O(n)$**
 - c. $O(n^2)$
 - d. $O(2n)$

4. (3 Points) In _____, the left and right subtrees of any node have heights that differ by at most 1.
 - a. all trees
 - b. all binary trees
 - c. n -ary trees
 - d. balanced binary trees**

5. (3 Points) In an array based representation of a complete binary tree, which of the following represents the left child of node `tree[i]`?
 - a. `tree[i+2]`
 - b. `tree[i-2]`
 - c. `tree[2*i+1]`**
 - d. `tree[2*i+2]`

6. (3 Points) A graph is _____ if it has at least one pair of vertices without a path between them.
 - a) complete
 - b) disconnected**
 - c) connected
 - d) full

7. (20 Points) Given the following ListInterface:

```
public interface ListInterface {  
    public void add(Object obj);  
    public boolean add(Object obj, int index);  
    public Object getObject(int index);  
    public boolean remove(int index);  
}
```

The correct array-based implementation:

```
public class ArrayList implements ListInterface {  
    private int tail = 0;  
    private Object[] arrayList = new Object[10000];  
  
    private void moveElementsToAdd(int begin, int end) {  
        for (int i = end ; i >= begin ; i-- ) {  
            arrayList[i+1] = arrayList[i];  
        }  
    }  
  
    private void moveElementsToRemove(int begin, int end) {  
        for (int i = begin ; i <= end ; i++ ) {  
            arrayList[i-1] = arrayList[i];  
        }  
    }  
  
    public void add(Object obj) {  
        if (tail < arrayList.length) {  
            arrayList[tail++] = obj;  
        }  
    }  
  
    public boolean add(Object obj, int index) {  
        if ((index <= tail) && (tail < arrayList.length)) {  
            moveElementsToAdd(index, tail-1);  
            arrayList[index] = obj;  
            tail++;  
            return true;  
        }  
        return false;  
    }  
  
    public Object getObject(int index) {  
        if (index <= tail) {  
            return arrayList[index];  
        }  
        return null;  
    }  
  
    public boolean remove(int index) {  
        if (index <= tail) {  
            moveElementsToRemove(index+1, tail-1);  
            tail--;  
            return true;  
        }  
        return false;  
    }  
}
```

8. (40 Points) The correct BinarySearchTree implementation is:

```
public class BinarySearchTree implements
BinarySearchTreeInterface {
    private TreeNode root = null;

    @Override
    public boolean isEmpty() {
        return (root == null);
    }

    @Override
    public void makeEmpty() {
        root = null;
    }

    @Override
    public void insert(TreeItem item) {
        root = insertItem(root, item);
    }

    private TreeNode insertItem(TreeNode node,
                                TreeItem newItem) {
        TreeNode newSubtree;

        if (node == null) {
            node = new TreeNode(newItem);
            return node;
        }

        if (newItem.compareTo(node.getItem()) < 0) {
            newSubtree =
insertItem(node.getLeftChild(), newItem);
            node.setLeftChild(newSubtree);
            return node;
        } else {
            newSubtree =
insertItem(node.getRightChild(), newItem);
            node.setRightChild(newSubtree);
            return node;
        }
    }
}
```

```
@Override
public TreeItem retrieve(int key) {
    return retrieveItem(root, key);
}

private TreeItem retrieveItem(TreeNode node,
                              int key) {
    TreeItem treeItem;
    TreeItem compareItem = new TreeItem(key);
    if (node == null) {
        treeItem = null;
    } else if
(compareItem.compareTo(node.getItem()) == 0) {
        treeItem = node.getItem();
    } else if
(compareItem.compareTo(node.getItem()) < 0) {
        treeItem =
retrieveItem(node.getLeftChild(), key);
    } else {
        treeItem =
retrieveItem(node.getRightChild(), key);
    }
    return treeItem;
}
}
```

9. (20 Points) The correct method for merging two arrays:

```
public void merge(T[]a, T[]b, T[]c) {
    int firstA = 0;
    int lastA = a.length - 1;
    int firstB = 0;
    int lastB = b.length - 1;

    int cIndex = 0;

    while ((firstA <= lastA) && (firstB <= lastB)) {
        if (a[firstA].compareTo(b[firstB]) < 0) {
            c[cIndex] = a[firstA++];
        } else {
            c[cIndex] = b[firstB++];
        }
        cIndex++;
    } // end while

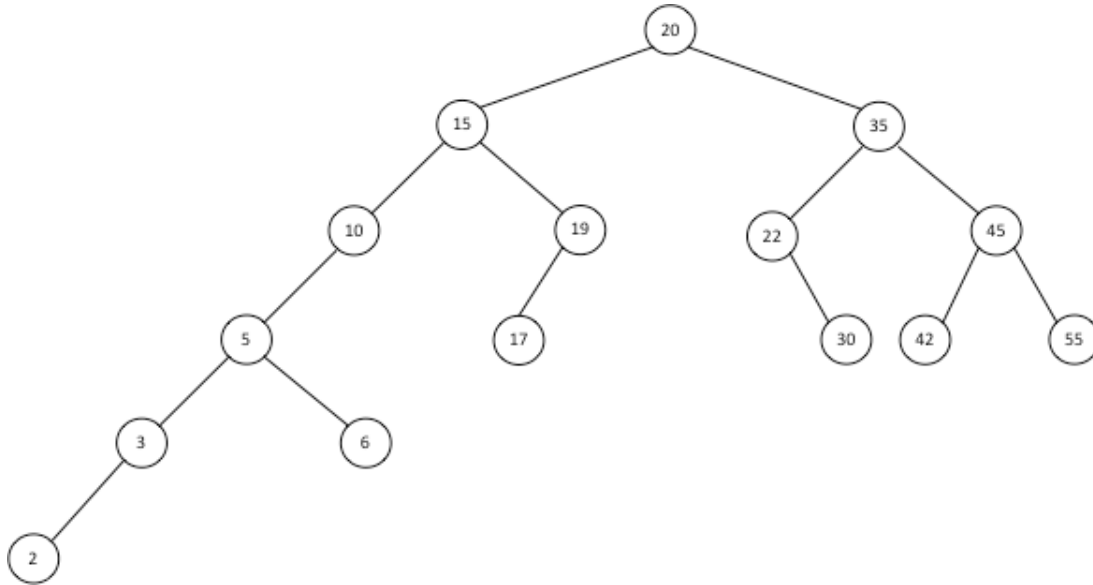
    while (firstA <= lastA) {
        c[cIndex++] = a[firstA++];
    } // end while

    while (firstB <= lastB) {
        c[cIndex++] = b[firstB++];
    } // end while
}
```

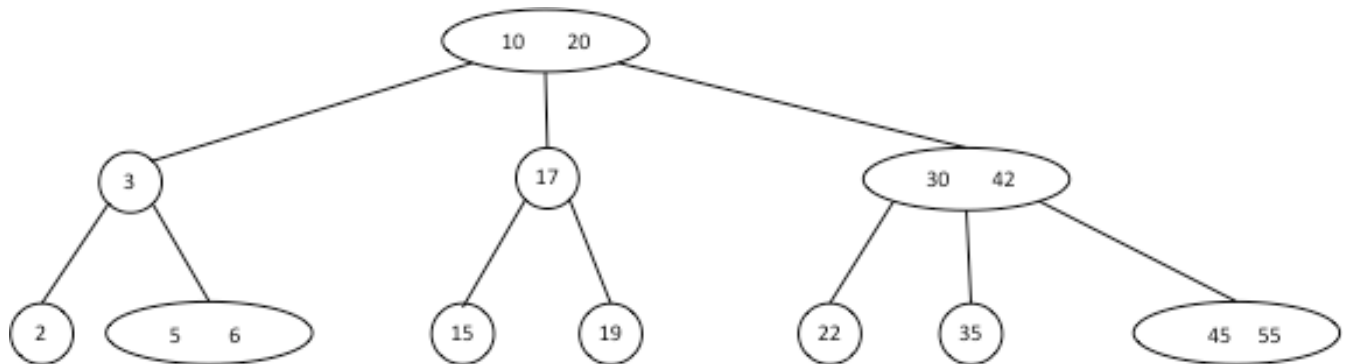
Solutions
Version 1

10. (16 Points) The following list of numbers: 20, 15, 35, 10, 5, 3, 19, 22, 30, 45, 2, 6, 42, 55, 17 inserted in the given order into:

a. (4 Points) Into a Binary Search Tree produces the following tree:

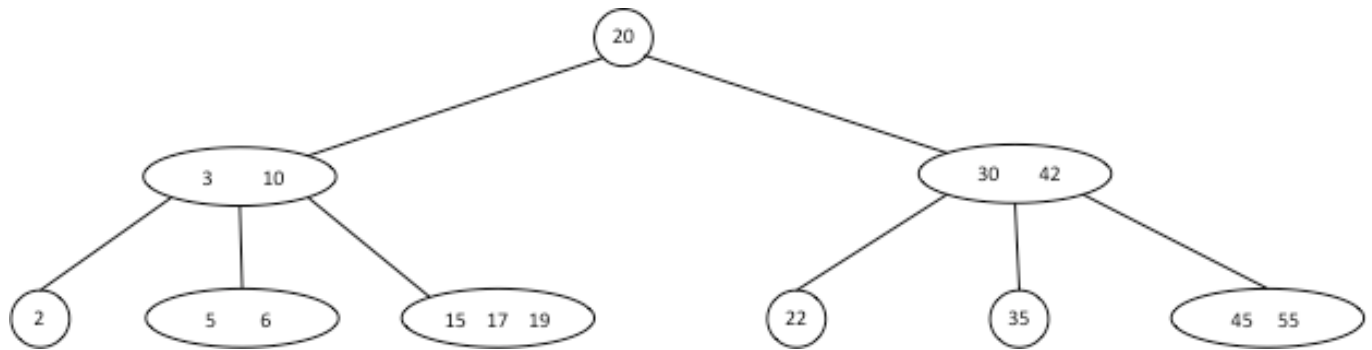


b. (4 Points) Into a 2-3 Tree produces the following tree:



Solutions
Version 1

c. (4 Points) Into a 2-3-4 Tree produces the following tree:



d. (4 Points) The numbers in the following order produces a full Binary Search Tree:

19, 6, 3, 2, 5, 15, 10, 17, 35, 22, 20, 30, 45, 42, 55

Solutions
Version 2

1. (3 Points) A superclass method can be accessed by a subclass, even though it has been overridden by the subclass, by using the _____ reference.
 - a. **super**
 - b. final
 - c. static
 - d. new

2. (3 Points) Assuming a linked list of n nodes, the code fragment:

```
Node curr = head;
while (curr != null) {
    System.out.println(curr.getItem());
    curr.setNext(curr.getNext());
} // end while
```

requires _____ comparisons.
 - a. n
 - b. $n - 1$
 - c. **$n + 1$**
 - d. 1

3. (3 Points) The value of which of the following growth-rate functions grows the fastest?
 - a. $O(n)$
 - b. **$O(n^2)$**
 - c. $O(1)$
 - d. $O(\log_2 n)$

4. (3 Points) In a _____ of height h , all nodes that are at a level less than h have two children each.
 - a. general tree
 - b. binary tree
 - c. **full binary tree**
 - d. complete binary tree

5. (3 Points) In an array based representation of a complete binary tree, which of the following represents the right child of node $tree[i]$?
 - a. $tree[i+2]$
 - b. $tree[i-2]$
 - c. $tree[2*i+1]$
 - d. **$tree[2*i+2]$**

6. (3 Points) The edges in a _____ indicate a direction.
 - a. graph
 - b. multigraph
 - c. **digraph**
 - d. spanning tree

Solutions
Version 2

7. (20 Points) Given the following ListInterface, the correct reference-based implementation is:

```
public interface ListInterface {
    public void add(Object obj);
    public boolean add(Object obj, int index);
    public Object getObject(int index);
    public boolean remove(int index);
}
```

//-----

```
public class Node {
    private Object object;
    private Node next;

    public Node(Object object) {
        this.object = object;
        this.next = null;
    }
    public Node getNext() {
        return next;
    }
    public void setNext(Node next) {
        this.next = next;
    }
    public Object getObject() {
        return object;
    }
}
```

//-----

```
public class LinkedList implements ListInterface {
    private Node head = null;
    private Node tail = null;
    private int listSize = 0;

    public void add(Object obj) {
        Node newNode = new Node(obj);

        if (head == null) {
            head = newNode;
        } else {
            tail.setNext(newNode);
        }
        tail = newNode;
        listSize++;
    }

    public Object getObject(int index) {
        Object obj = null;
        Node curNode = head;

        if (index < listSize && head != null) {
            for (int i = 0; i < index; i++) {
                curNode = curNode.getNext();
            }
            obj = curNode.getObject();
        }
        return obj;
    }
}
```

```
public boolean add(Object obj, int index) {
    boolean rc = false;
    Node newNode = new Node(obj);
    Node curNode = head;

    if (index == 0) {
        if (head == null) {
            tail = newNode;
        }
        newNode.setNext(head);
        head = newNode;
        listSize++;
        rc = true;
    } else if (index == listSize) {
        add(obj);
        rc = true;
    } else if (index < listSize) {
        for (int j = 1; j < index; j++) {
            curNode = curNode.getNext();
        }
        newNode.setNext(curNode.getNext());
        curNode.setNext(newNode);
        listSize++;
        rc = true;
    }
    return rc;
}

public boolean remove(int index) {
    boolean result = false;
    Node curNode = head;
    Node prevNode = null;

    if (index < listSize) {
        if (index == 0) {
            head = head.getNext();
            result = true;
        } else {
            for (int i = 0; i < index; i++) {
                prevNode = curNode;
                curNode = curNode.getNext();
            }
            prevNode.setNext(curNode.getNext());
            if (index == (listSize - 1)) {
                tail = prevNode;
            }
            result = true;
        }
        listSize--;
    }
    return result;
}
```


8. (40 Points) The correct BinarySearchTree implementation is:

```
public class BinarySearchTree implements
BinarySearchTreeInterface {
    private TreeNode root = null;

    @Override
    public boolean isEmpty() {
        return (root == null);
    }

    @Override
    public void makeEmpty() {
        root = null;
    }

    @Override
    public void insert(TreeItem item) {
        root = insertItem(root, item);
    }

    private TreeNode insertItem(TreeNode node,
                                TreeItem newItem) {
        TreeNode newSubtree;

        if (node == null) {
            node = new TreeNode(newItem);
            return node;
        }

        if (newItem.compareTo(node.getItem()) < 0) {
            newSubtree =
insertItem(node.getLeftChild(), newItem);
            node.setLeftChild(newSubtree);
            return node;
        } else {
            newSubtree =
insertItem(node.getRightChild(), newItem);
            node.setRightChild(newSubtree);
            return node;
        }
    }
}
```

```
@Override
public TreeItem retrieve(int key) {
    return retrieveItem(root, key);
}

private TreeItem retrieveItem(TreeNode node,
                                int key) {
    TreeItem treeItem;
    TreeItem compareItem = new TreeItem(key);
    if (node == null) {
        treeItem = null;
    } else if
(compareItem.compareTo(node.getItem()) == 0) {
        treeItem = node.getItem();
    } else if
(compareItem.compareTo(node.getItem()) < 0) {
        treeItem =
retrieveItem(node.getLeftChild(), key);
    } else {
        treeItem =
retrieveItem(node.getRightChild(), key);
    }
    return treeItem;
}
}
```

9. (20 Points) The correct method for merging two arrays:

```
public void merge(T[]a, T[]b, T[]c) {
    int firstA = 0;
    int lastA = a.length - 1;
    int firstB = 0;
    int lastB = b.length - 1;

    int cIndex = 0;

    while ((firstA <= lastA) && (firstB <= lastB)) {
        if (a[firstA].compareTo(b[firstB]) < 0) {
            c[cIndex] = a[firstA++];
        } else {
            c[cIndex] = b[firstB++];
        }
        cIndex++;
    } // end while

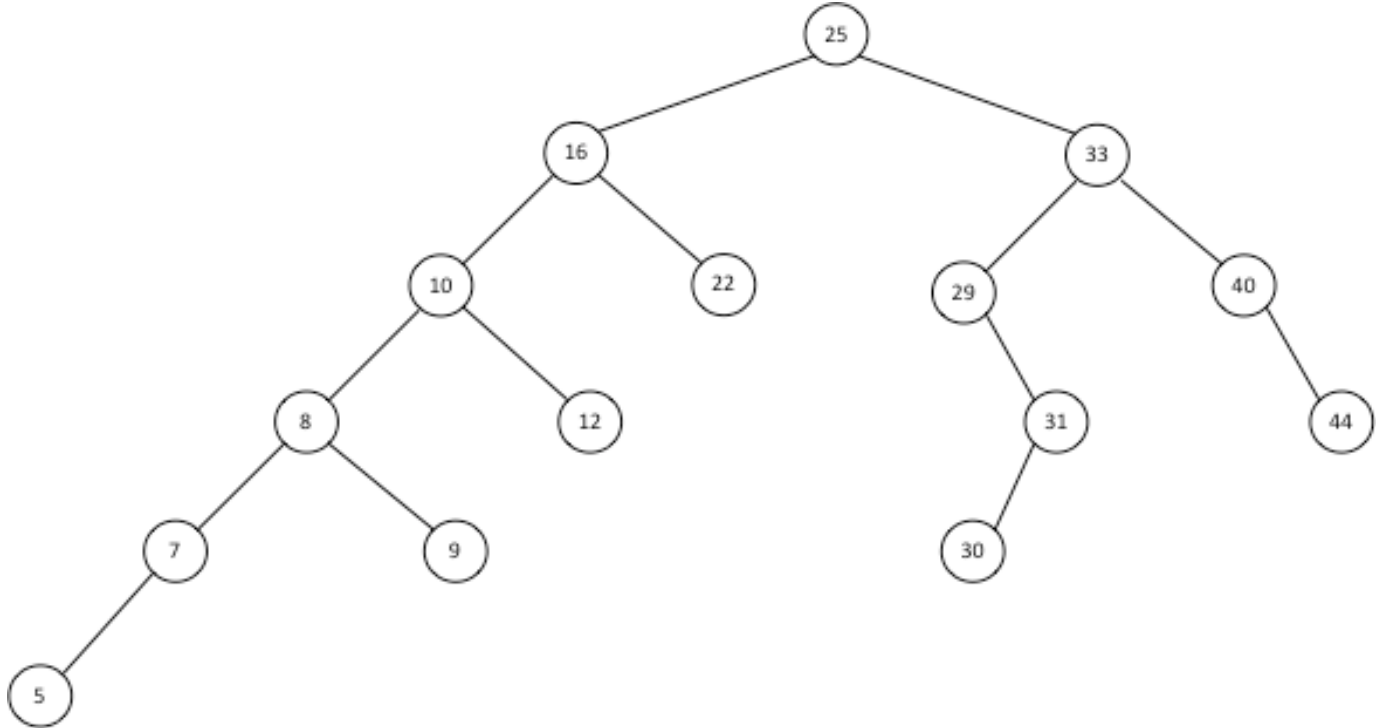
    while (firstA <= lastA) {
        c[cIndex++] = a[firstA++];
    } // end while

    while (firstB <= lastB) {
        c[cIndex++] = b[firstB++];
    } // end while
}
```

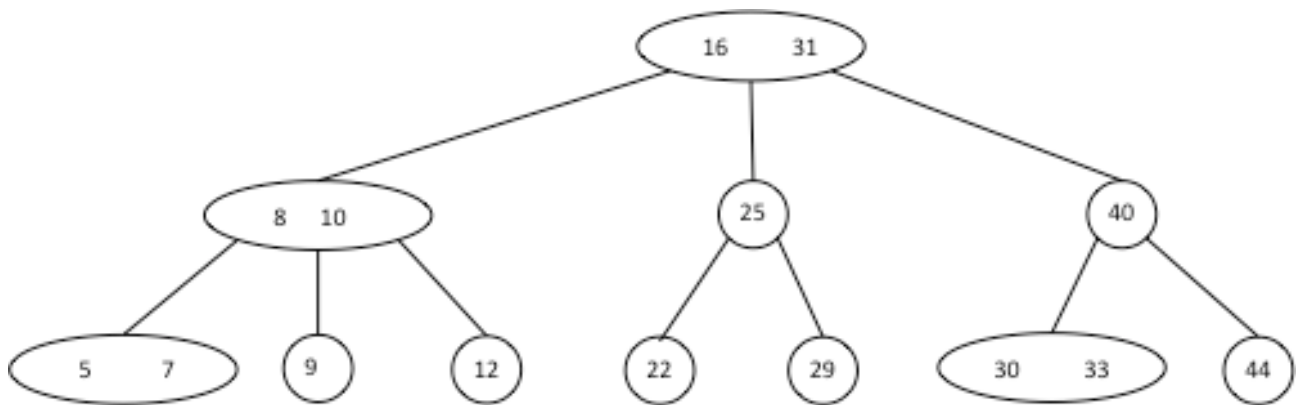
Solutions
Version 2

10. (16 Points) The following list of numbers: 25, 16, 33, 22, 10, 8, 7, 9, 5, 12, 29, 31, 40, 44, 30 inserted in the given order into:

a. (4 Points) Into a Binary Search Tree produces the following tree:

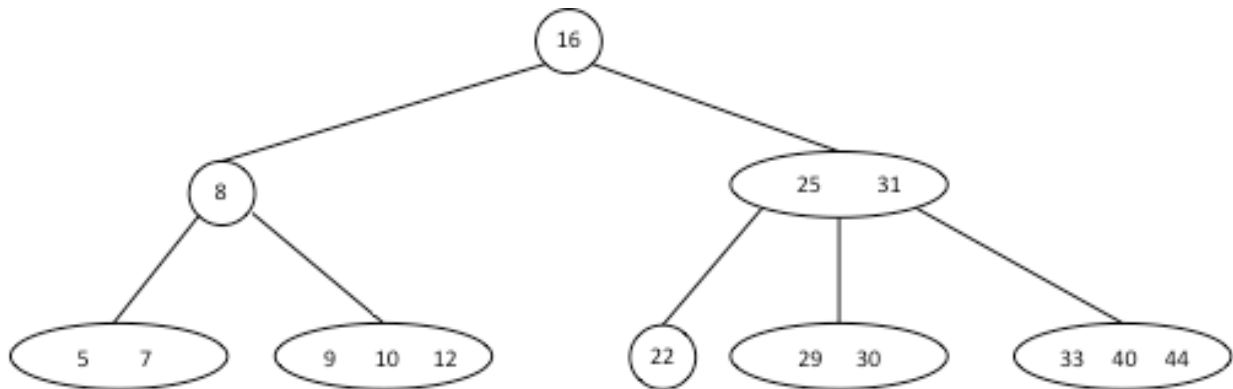


b. (4 Points) Into a 2-3 Tree produces the following tree:



Solutions
Version 2

c. (4 Points) Into a 2-3-4 Tree produces the following tree:



d. (4 Points) The numbers in the following order produces a full Binary Search Tree:

22, 9, 7, 5, 8, 12, 10, 16, 31, 29, 25, 30, 40, 33, 44