

## Instructions

- Answer **all** questions on the yellow paper.
- **One** question per page.
- Use only **one** side of the yellow paper.

1. (20 Points) Given the `LinkedList` class that has the following attributes:

```
private Node<I> head = null;
private Node<I> tail = null;
private int listSize = 0;
```

Where `I` extends `Comparable<? super I>>`. Re-write the following methods from the `LinkedList` class and **fix all 10 logical errors**:

```
// add the given element at the given index
// return true if successful, false otherwise
public boolean add(I element, int index) {
    boolean rc = false;
    Node<I> newNode = new Node<I>(element);
    Node<I> curNode = tail;

    if (index == 0) {
        if (head == null) {
            tail = newNode;
        }
        newNode.setNext(head);
        tail = newNode;
        listSize++;
        rc = true;
    } else if (index > listSize) {
        add(element);
        rc = true;
    } else if (index < listSize) {
        for (int j = 1 ; j < index ; j++ ) {
            curNode = curNode.getNext();
        }
        newNode.setNext(curNode);
        curNode.setNext(newNode);
        listSize--;
        rc = true;
    }
    return rc;
}
```

```
// remove the element at the specified index
// return true if successful, false otherwise
public boolean remove(int index) {
    boolean rc = false;
    Node<I> curNode = head;
    Node<I> prevNode = null;

    if (index > listSize) {
        if (index == 0) {
            tail = head.getNext();
            rc = true;
        } else {
            for (int i = 0 ; i < index ; i++ ){
                prevNode = curNode;
                curNode = prevNode.getNext();
            }
            prevNode.setNext(curNode.getNext());
            if (index == (listSize - 1)) {
                head = prevNode;
            }
            rc = true;
        }
        listSize--;
    }
}
```

2. (30 Points) Write a method to reverse the contents of a list. The **List** class implements the **ListInterface** given below. You can also assume that you have access to a **Queue** class that implements the **QueueInterface** below and a **Stack** class that implements the **StackInterface** below.

```
public interface ListInterface<I>
{
    public int size();
    public boolean isEmpty();
    public void add(I e);
    public I get(int index);
    public void remove(int index);
}

public interface QueueInterface<I>
{
    public int size();
    public boolean isEmpty();
    public void enqueue(I e);
    public I peek();
    public I dequeue();
    public I dequeue(int index);
}

public interface StackInterface<I>
{
    public int size();
    public boolean isEmpty();
    public void push(I e);
    public I peek();
    public I pop();
}
```

The method should accept a **List** as a parameter and return the reversed **List**. The method should have the following signature:

```
public List<I> reverseList(List<I> list) {
}
}
```

3. (20 Points) Given an array of **TreeItem** elements that is sorted in ascending order, write a method to create a balanced **BinarySearchTree** from all the elements of the array. The **BinarySearchTree** implements the **BinarySearchTreeInterface** given below. Your method should have the following signature:

```
public BinarySearchTree<K,V> createBalancedTree(TreeItem<K,V>[] items) {

}
```

**BinarySearchTreeInterface**, **TreeNode** and **TreeItem** are as follows:

```
public interface BinarySearchTreeInterface <K extends Comparable<? super K>, V> {
    public TreeNode<K, V> getRoot();
    public void setRoot(TreeNode<K, V> root);
    public boolean isEmpty();
    public TreeItem<K,V> getRootItem();
    public TreeItem<K,V> find(K key);
    public void insert(TreeItem<K,V> treeItem);
    public void delete(K key);
}
```

```
public class TreeNode
    <K extends Comparable<? super K>, V> {
    private TreeItem<K,V> treeItem;
    private TreeNode<K,V> leftChild;
    private TreeNode<K,V> rightChild;
    private TreeNode<K,V> parent;

    public TreeNode(TreeItem<K,V> treeItem) {
        this.treeItem = treeItem;
        this.leftChild = null;
        this.rightChild = null;
        this.parent = null;
    }

    public TreeNode<K, V> getLeftChild() {
        return leftChild;
    }
    public void setLeftChild(TreeNode<K,V> leftChild) {
        this.leftChild = leftChild;
    }

    public TreeNode<K, V> getRightChild() {
        return rightChild;
    }
    public void setRightChild(TreeNode<K,V> rightChild) {
        this.rightChild = rightChild;
    }

    public TreeNode<K, V> getParent() {
        return parent;
    }
    public void setParent(TreeNode<K, V> parent) {
        this.parent = parent;
    }

    public TreeItem<K, V> getTreeItem() {
        return treeItem;
    }
    public void setTreeItem(TreeItem<K, V> treeItem) {
        this.treeItem = treeItem;
    }
}
```

```
public class TreeItem
    <K extends Comparable<? super K>, V> {
    private K key;
    private V value;

    public TreeItem(K key, V value) {
        this.key = key;
        this.value = value;
    }

    public K getKey() {
        return key;
    }

    public V getValue() {
        return value;
    }

    public void setValue(V value) {
        this.value = value;
    }
}
```

4. (20 Points) A heap can be represented by an array **heapArray**.

An element at index **n** in **heapArray** has its left child at index  $2n + 1$  and its right child at index  $2n + 2$ . Also, an element at index **m** in **heapArray** has its parent at index  $(m - 1) / 2$ .

A Max-Heap is a heap where every node in the heap is bigger than its children.

Given a random array **heapArray**, write the **heapify()** method that converts **heapArray** into a Max-Heap. You can assume the following:

```
T heapArray[];
```

And

```
<T extends Comparable<? super T>>
```

The method should have the following signature:

```
private void heapify() {  
}
```

5. (20 Points) Given the following list of numbers:

80, 70, 10, 100, 90, 130, 60, 120, 50, 110, 20, 30, 140, 150, 40

being inserted in the given order.

- a. (5 Points) Draw the resulting Binary Search Tree.
- b. (5 Points) Draw the resulting 2-3 Tree.
- c. (5 Points) Draw the resulting 2-3-4 Tree.
- d. (5 Points) What order should the numbers be inserted in order to obtain a Full Binary Search Tree?