

restart

$$\textcolor{teal}{f} := t \rightarrow \cos(t^2) \quad \textcolor{blue}{t \rightarrow \cos(t^2)} \quad (1)$$

evalf(f(3))

$$-0.9111302619 \quad (2)$$

with(Student[Calculus1])

[AntiderivativePlot, AntiderivativeTutor, ApproximateInt, ApproximateIntTutor, ArcLength, (3)

ArcLengthTutor, Asymptotes, Clear, CriticalPoints, CurveAnalysisTutor, DerivativePlot,
DerivativeTutor, DiffTutor, ExtremePoints, FunctionAverage, FunctionAverageTutor,
FunctionChart, FunctionPlot, GetMessage, GetNumProblems, GetProblem, Hint,
InflectionPoints, IntTutor, Integrand, InversePlot, InverseTutor, LimitTutor,
MeanValueTheorem, MeanValueTheoremTutor, NewtonQuotient, NewtonsMethod,
NewtonsMethodTutor, PointInterpolation, RiemannSum, RollesTheorem, Roots, Rule, Show,
ShowIncomplete, ShowSolution, ShowSteps, Summand, SurfaceOfRevolution,
SurfaceOfRevolutionTutor, Tangent, TangentSecantTutor, TangentTutor,
TaylorApproximation, TaylorApproximationTutor, Understand, Undo, VolumeOfRevolution,
VolumeOfRevolutionTutor, WhatProblem]

RiemannSum(f(t), t = 0.0 .. 1, method = upper, output = value, partition = 100)

$$0.3383500000 \quad (4)$$

F := x → RiemannSum(f(t), t = 0 .. x, method = upper, output = value, partition = 1000)

x → Student:-Calculus1:-RiemannSum(f(t), t = 0 .. x, method = upper, output = value, partition (5)
= 1000)

$$F(1) \quad 0.3337147341 \quad (6)$$

$$F(2) \quad 0.4638088253 \quad (7)$$

$$F(3) \quad 9.003437870 \quad (8)$$

$$dx := .001 \quad 0.001 \quad (9)$$

$$DF3 := \frac{(F(3 + dx) - F(3))}{dx} \quad -0.9057153000 \quad (10)$$